

## Part I (due Friday, March 8 at the beginning of class)

I updated DW 20 reading to not include determinants (I'm sorry—I copied an old example too quickly!); the only change is that we can just row reduce the matrix to see that its rref is  $I$  and thus we know the matrix is invertible.

**Definition 1.** A nonzero vector space  $V$  is called finite-dimensional if it contains a finite set of vectors  $\{\vec{v}_1, \vec{v}_2, \dots, \vec{v}_n\}$  that forms a basis for  $V$ . If no such set exists,  $V$  is called infinite-dimensional. We also regard the vector space  $\{\vec{0}\}$  as finite-dimensional.

**Example 1.** • finite-dimensional:  $\mathbb{R}^n$ ,  $M_{m \times n}$ , etc.

• infinite-dimensional:  $F(-\infty, \infty)$ ,  $C[a, b]$ , etc.

**Definition 2.** If  $V$  has a basis with  $n$  vectors, then we say that  $V$  is  $n$ -dimensional.

### Reading Question(s)

1. What dimension is the vector space  $P_3(x)$ ? What about  $M_{2 \times 2}$ ?

## Part II (prepare for Friday, March 8)

Finish the examples on the Bases and Coordinate Vectors handout.

## Part III: Homework (due Friday, March 15 at the beginning of class)

1. True or False (if true, prove; if false, give an explained counterexample):
  - (a) In  $P_3$ , the set of all polynomials of degree three or less with real coefficients, every set with more than three vectors is linearly independent.
  - (b) If  $\{\vec{v}_1, \vec{v}_2\}$  is linearly independent and  $\vec{v}_3 \notin \text{span}(\{\vec{v}_1, \vec{v}_2\})$ , then  $\{\vec{v}_1, \vec{v}_2, \vec{v}_3\}$  is linearly independent.
  - (c) If  $\vec{u}$ ,  $\vec{v}$ , and  $\vec{w}$  are vectors in a vector space  $V$ , then  $\{\vec{u} - \vec{v}, \vec{v} - \vec{w}, \vec{w} - \vec{u}\}$  is linearly dependent.
  - (d) The polynomials  $(x - 1)(x + 2)$ ,  $x(x + 2)$ , and  $x(x - 1)$  are linearly independent.

## Running list of vocabulary words that could be a quiz word

- linear equation
- system of linear equations
- linear combination of a set of vectors
- span of a set of vectors

- linearly independent
- linearly dependent
- reduced row echelon form
- pivot
- homogeneous system
- free variable
- row equivalent
- consistent system
- inconsistent system
- trace of a matrix
- transpose of a matrix
- inverse of a matrix
- elementary matrix
- transformation
- domain
- codomain
- range
- vector space (I will not ever ask you to define this on a quiz—the definition is way too long—but you should make sure you know what makes something a vector space)
- subspace