## Part I (due Monday, February 19 at the beginning of class)

Think about whether the set

$$V = \left\{ \begin{bmatrix} a & b \\ c & d \end{bmatrix} : a, b, c, d \in \mathbb{R} \right\}$$

satisfies the vector space axioms we talked about in class Friday. You don't need to turn anything in for this, but come prepared to discuss it.

Here's the definition again:

**Definition 1.** Let V be a nonempty set of objects on which addition and scalar multiplication are defined. If the following axioms hold for all  $\vec{u}$ ,  $\vec{v}$ , and  $\vec{w}$  in V and for all scalars c and d, then V is a vector space (and the objects in V are vectors).

- 1.  $\vec{v}, \vec{w} \in V$  implies  $\vec{v} + \vec{w} \in V$  (closure under addition)
- 2.  $\vec{v} + \vec{w} = \vec{w} + \vec{v}$  (addition is commutative)
- 3.  $\vec{u} + (\vec{v} + \vec{w}) = (\vec{u} + \vec{v}) + \vec{w}$  (addition is associative)
- 4. There is a  $\vec{0} \in V$  such that  $\vec{0} + \vec{v} = \vec{v} + \vec{0} = \vec{v}$  (additive identity)
- 5. For each  $\vec{v} \in V$ , there exists a vector  $-\vec{v} \in V$  such that  $\vec{v} + (-\vec{v}) = -\vec{v} + \vec{v} = \vec{0}$  (additive inverse)
- 6.  $c\vec{v} \in V$  (closure under scalar multiplication)
- 7.  $c(\vec{v} + \vec{w}) = c\vec{v} + c\vec{w}$  (distributivity of scalar multiplication over addition)
- 8.  $(c+d)\vec{v} = c\vec{v} + d\vec{v}$  (another form of distributivity)
- 9.  $c(d\vec{v}) = (cd)\vec{v}$  (associativity of scalar multiplication)
- 10.  $1\vec{v} = \vec{v}$  (scalar multiplicative identity)

## Part II (prepare for Wednesday, February 21)

There will be a WeBWorK assignment posted by Friday night.

## Part III: Homework (due Wednesday, February 21 at the beginning of class)

- 1. For each of the following, give an explained example or explain why such an example does not exist.
  - (a) a one-to-one transformation from  $\mathbb{R}^3$  to  $\mathbb{R}^4$
  - (b) an onto transformation from  $\mathbb{R}^3$  to  $\mathbb{R}^4$
  - (c) a one-to-one but not onto transformation from  $\mathbb{R}^4$  to  $\mathbb{R}^4$

## Running list of vocabulary words that could be a quiz word

- linear equation
- system of linear equations
- linear combination of a set of vectors
- span of a set of vectors
- linearly independent
- linearly dependent
- reduced row echelon form
- pivot
- homogeneous system
- free variable
- row equivalent
- consistent system
- inconsistent system
- trace of a matrix
- transpose of a matrix
- inverse of a matrix
- elementary matrix
- $\bullet \ {\rm transformation}$
- domain
- codomain
- range
- vector space (I will not ever ask you to define this on a quiz—the definition is way too long—but you should make sure you know what makes something a vector space)