Math 182: Calculus I Daily Work 24

Part I (due at the beginning of class Monday, November 3)

Read the following. No reading questions this time.

We now want to explore how the derivative of a function can help us understand what the original function looks like.

Definition 1. A function f(x) is called

- increasing on (a,b) if $f(x_1) \leq f(x_2)$ for all $x_1, x_2 \in (a,b)$ such that $x_1 < x_2$
- decreasing on (a,b) if $f(x_1) \ge f(x_2)$ for all $x_1, x_2 \in (a,b)$ such that $x_1 < x_2$.

We say that f(x) is monotone on (a,b) if it is either decreasing or increasing on (a,b).

Theorem 1. Let f(x) be differentiable on (a,b).

- If f'(x) > 0 for $x \in (a,b)$, then f is increasing on (a,b).
- If f'(x) < 0 for $x \in (a,b)$, then f is decreasing on (a,b).

Part II: WeBWorK (due Saturday, November 8, by 11 PM)

Click here for your WeBWorK assignment. Complete the DW 24 WeBWorK assignment.

Part III: Homework Problems (due Wednesday, November 5 at the beginning of class)

- 1. Suppose that f(0) = 1 and $f'(x) \le 2$ for every value of x. Use the Mean Value Theorem to determine the largest possible value for f(4). Make sure to explain why the Mean Value Theorem applies (why f(x) satisfies the hypotheses of the MVT).
- 2. Show that the function $f(x) = x^5 + 6x + c$ has at most one real root in the interval [-1, 1].

Integration Assignment Reminder

The due date for Integration Assignment 4 is now Monday, November 3.